

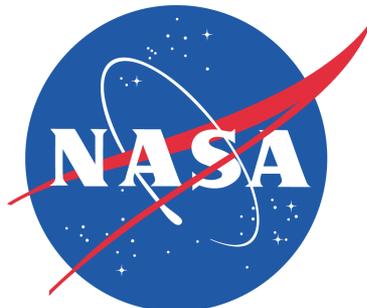
# A Gridded Product That Uses Dynamical and Thermodynamical Constraints

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With thanks to  
NASA OVWST, NASA NEWS, and NOAA/COD



# Motivation

- Complete (over water) in space and time
  - This is expected for ease of use
- No boundary condition forced at the sea edge
  - Improved near shore winds
  - Improved high latitude storms near ice
- Reproduction of observed dependence on SST gradients (assumed to be air temperature gradients)
  - This has a substantial impact on upwelling and air/sea fluxes
  - Removes seasonal and regional biases
- Push spatial/temporal resolution as far as reasonable
- The observing system should not be apparent in the product

# Our General Approach

- A gridded product based on
  - A misfit to observations
    - Vector winds, scalar winds
    - SST, air temperature, surface pressure, surface humidity,
  - Misfit to a background field (from NWP)
  - A misfit to a physical model linking variables
    - A hard constraint would force an exact match to this model
    - A soft constrain is more realistic since we don't believe the model is perfect, and misses smaller scales
- The hard part is developing a realistic model!
- First guess is based on NWP and the physical model

# Our Approach for the Model

- We have combined two models from oceanography, and applied them to the atmosphere
  - Stommel (1953) Geostrophic flow
    - 1. Vertically uniform eddy diffusivity ( $K$ ).
    - 2. Zero shear, stress ( $K = \text{const}$ ) at  $z = -H$  and match stress at surface ( $du/dz = \tau(0)/(\rho K)$ )
    - 3. Zonal wind stress uniform in  $y$  ( $\text{curl}(\tau) = 0$ ) implying that the vertically integrated transport is zero (Integral  $-H$  to 0 of  $u(z) = 0$ )
    - 4. No “fronts”  $\text{Grad}(T) = 0$ .
  - Lagerloef and Bonjean (2002) links Geostr., Ekman, surface
    - Removes assumptions 3 and 4
  - Coupling with a log profile fixes the problems with (1) and (2)

*These are not realistic assumptions for our application – all must be removed*

# The Solution

- Skipping many steps

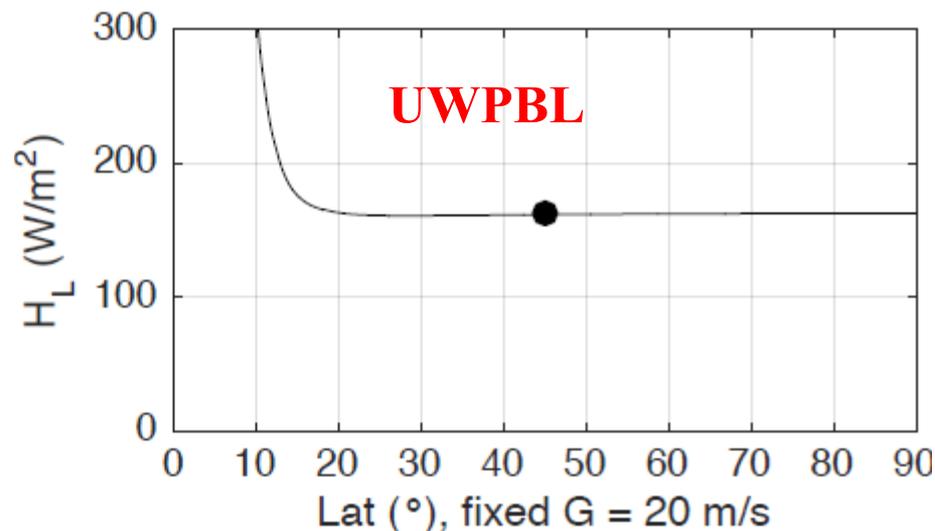
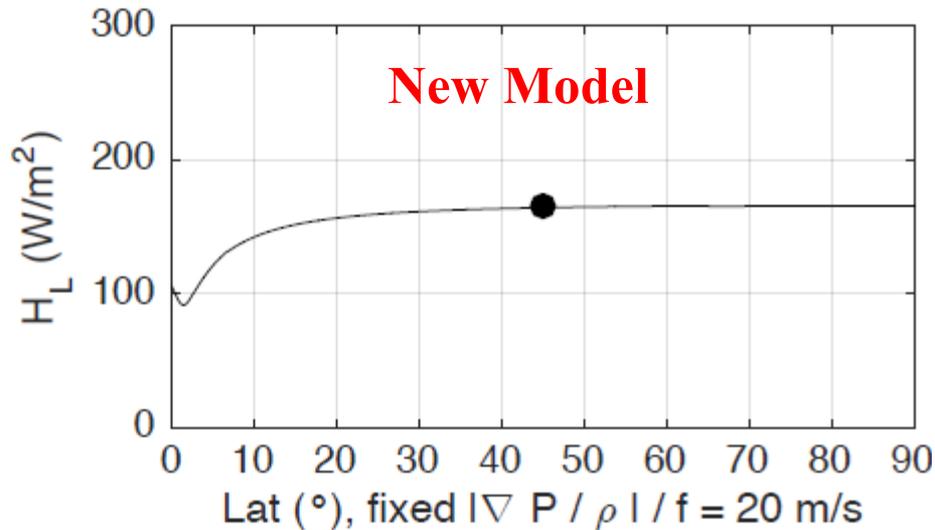
$$\mathbf{U}(z) = \mathbf{U}(h_p) + (z - h_p) \left( \frac{g \nabla T}{T_0} \frac{\left( (z - h_p)^2 - 3(H - h_p)^2 \right)}{6K} + \frac{\nabla p(h_p)}{\rho} \frac{(z + h_p - 2H)}{2K} \right) \quad (14)$$

where  $\mathbf{U}(h_p)$  is provided by the surface layer expression,

$$\mathbf{U}(h_p) = \frac{u^*}{k} \left( \ln(h_p / z_0) - \Psi(h_p / L) \right), \quad (15)$$

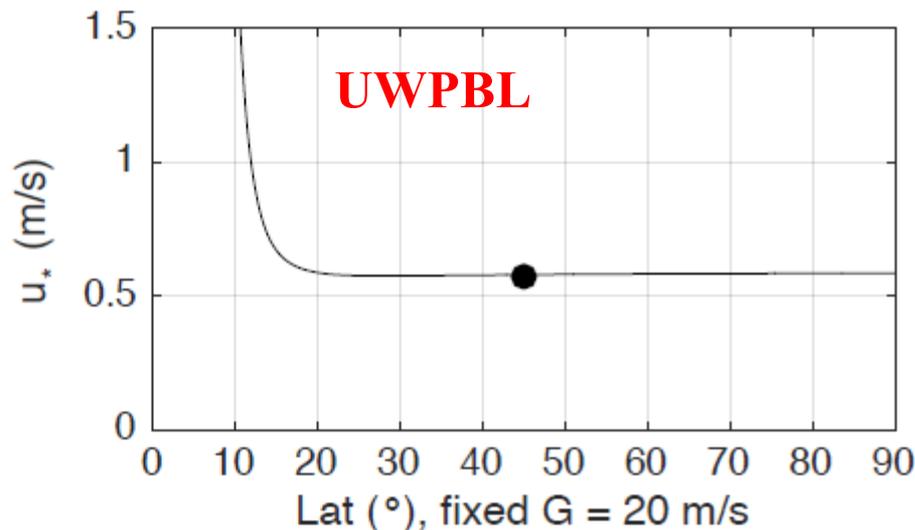
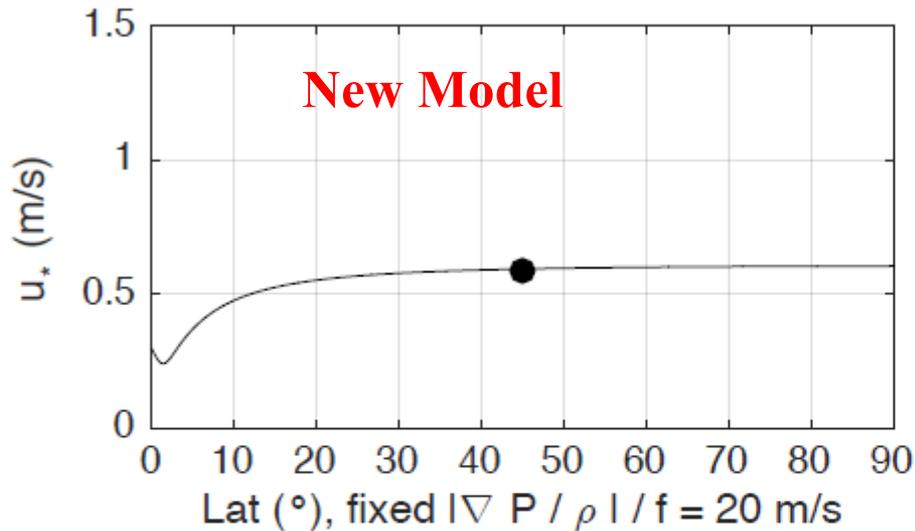
- Where (15) is the standard Boundary-layer log-layer solution
- (14) is a cubic Ekman layer solution at the equator
  - similar to Stommel's result,
  - a lot more flexible and widely applicable

# Sensitivity Analysis & Comparison to UWPBL: Latent Heat Flux



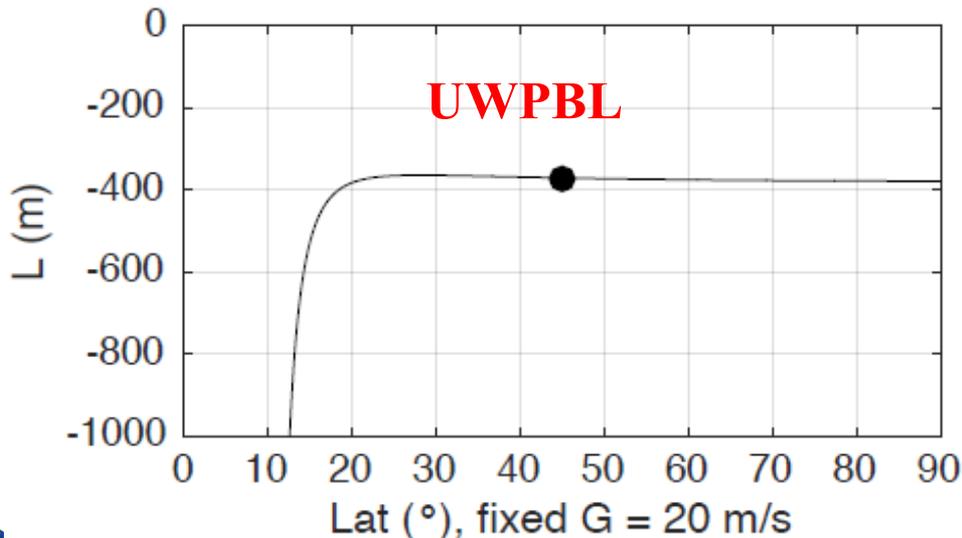
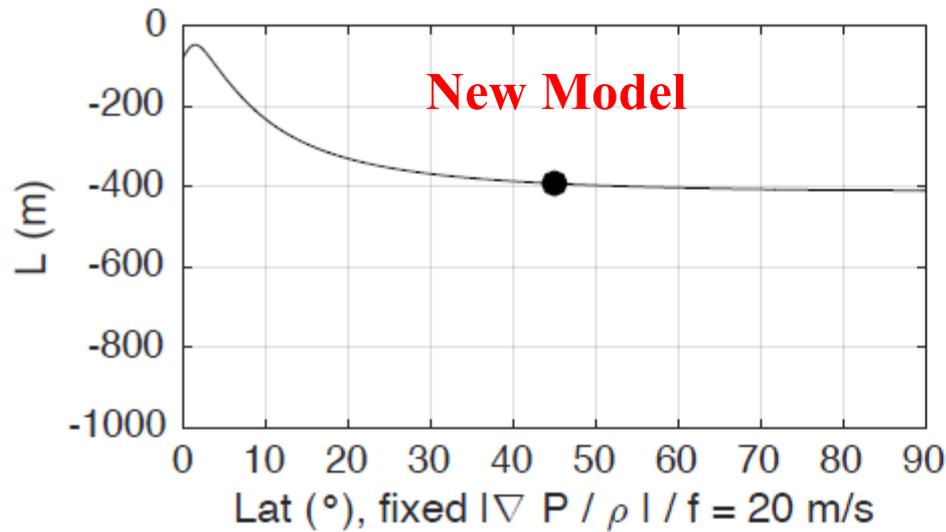
- Latent Heat Flux
- Caveat: the results are for the fuller physics version of the UWPBL.
- The light-physics tropical version of the UWPBL is more stable
- But does not have needed physics

# Sensitivity Analysis & Comparison to UWBPBL: Friction Velocity



- Reasonable input for unstable boundary-layer stratification
- The new model is quite stable
- UWPBL does not converge within  $8^{\circ}$  of the equator, and would give unfortunately large stress with about  $20^{\circ}$  of the equator

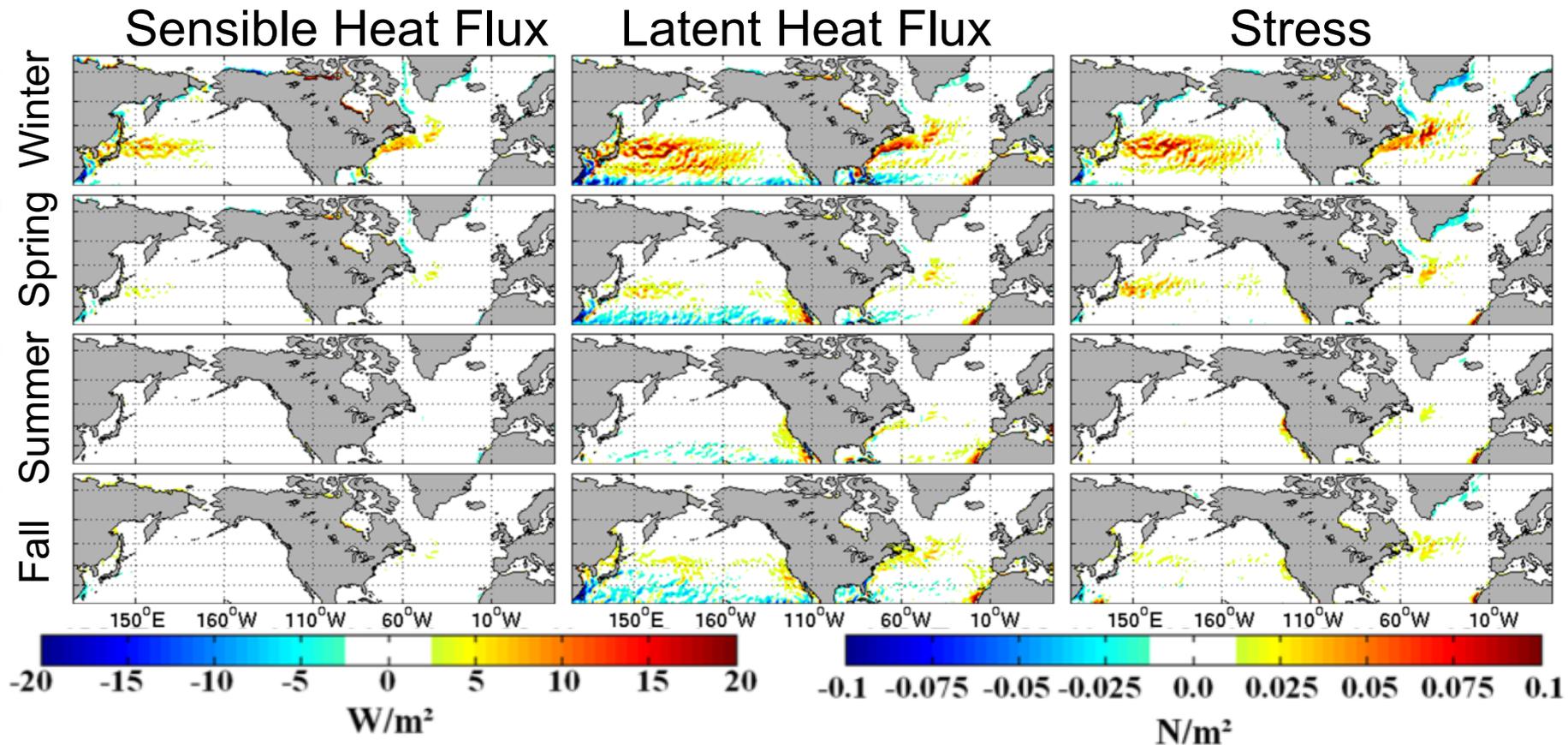
# Sensitivity Analysis & Comparison to UWPBL: M-O Scale Length



- M-O scale length is stable for new model
- Latitudinal dependence quite different depending on what is held constant
- UWPBL M-O length approaches negative infinity
  - Very deep boundary layer

# Preliminary Seasonal Results

## Flux Differences Relative to case with No SST Dependence



2002 – 2003 seasonal average differences in SHF (left), LHF (middle), and wind stress (right) for DJF (top row), MAM (2<sup>nd</sup> row), JJA (3<sup>rd</sup> row), and SON (bottom row)

*Courtesy John Steffen*

# Conclusions

- A purely statistical approach cannot achieve the desired spatial/temporal resolution without far more data than are available
- We believe that a physical model can be used to provide the far more connectivity between observations, and hence fill gaps and improve resolution
  - Like NWP, but far less sophisticated, and hopefully a better fit to the data (particularly in the tropics and the high latitudes)
  - Like NWP, other types of data are useful: speeds, SSTs, ....
  - While also producing consistent fields of surface fluxes
- Preliminary results (shown several meeting prior) support that the model contains the physics needed to have a reasonable dependence on temperatures and temperature gradients
- Unlike the UWPBL model, this model works globally with the same model for SST dependence

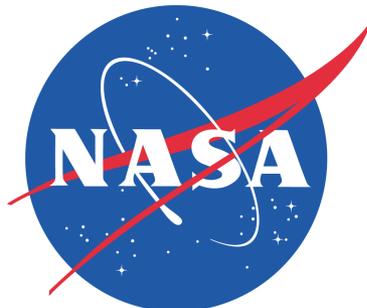
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# Backup Slides

# Solution

$$i f \mathbf{U} = -1 / \rho_0 \nabla p + K \frac{\partial^2 \mathbf{U}}{\partial z^2} \quad (1)$$

where:  $\nabla \equiv \partial / \partial x + i \partial / \partial y$

$$\mathbf{U} \equiv u + i v$$

The boundary conditions are that the stress vanishes at the top of the Ekman layer  $z = H$  and is matched to the surface layer stress at  $z = h_p$ .  $K$  is assumed constant, implying that the shear at the top of the Ekman layer vanishes. Our boundary conditions are

$$\partial \mathbf{U} / \partial z = 0 \quad z = H \quad (2)$$

$$\partial \mathbf{U} / \partial z = \mathbf{t} / (\rho_0 K) \quad z = h_p \quad (3)$$

where  $\mathbf{t}$  is the complex surface layer stress,  $\mathbf{t} = \tau^x + i \tau^y$ . The classical Ekman model would have taken the drag to vanish at  $z \rightarrow \infty$ , which with constant  $K$  gives

$$\frac{\partial^2 \mathbf{U}}{\partial z^2} \rightarrow 0, \quad z \rightarrow \infty.$$

# Solution Continued

The model Ekman layer includes a simplified buoyancy forcing in the vertical hydrostatic balance allowing for thermal wind.

$$1 / \rho_0 \partial p / \partial z = -g + g (T - T_0) / T_0 \quad (4)$$

where  $T_0$  is the surface temperature. Applying the  $\nabla$  operator to (4) gives

$$1 / \rho_0 \partial \nabla p / \partial z = g \nabla T / T_0 \quad (5)$$

- This is very important for modeling the impact of SST gradients

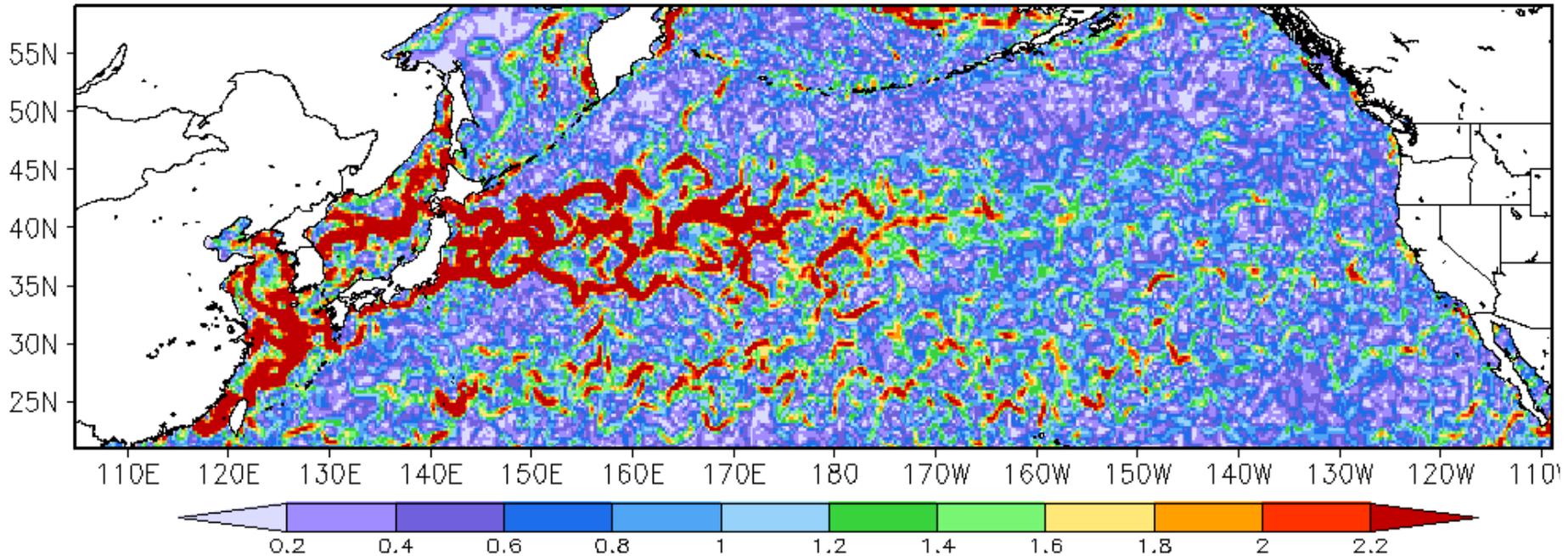
# Further Minor Caveats

- The new model is numerically unstable or overly sensitive if
  - The unstable boundary-layer is too shallow
    - Solution: set  $H \approx 1500\text{m}$
  - The stable boundary-layer is too deep
    - 3 to 5 solutions for deep layers
    - Solution: set  $H \approx 200\text{m}$
- At the suggested thicknesses, the results are very insensitive to the value of  $H$ .
- Alternatively, we could also use boundary-layer heights from NWP.

# Technical Details I

- Steady, horizontally uniform, two-layer model consisting of an upper Ekman layer that is matched to a surface layer below. The surface layer is a standard stratified Monin-Obukhov type layer extending from the surface to a height  $z = h_p$  where the matching to the Ekman layer occurs.
- The difference between this model and some other PBL models is structure of the Ekman layer. Rather than extending to  $z = \infty$ , the model Ekman layer occupies the region  $h_p < z < H$ , from the top of the surface layer to a *finite* height  $H$ .

# Example Reynolds SST Gradients

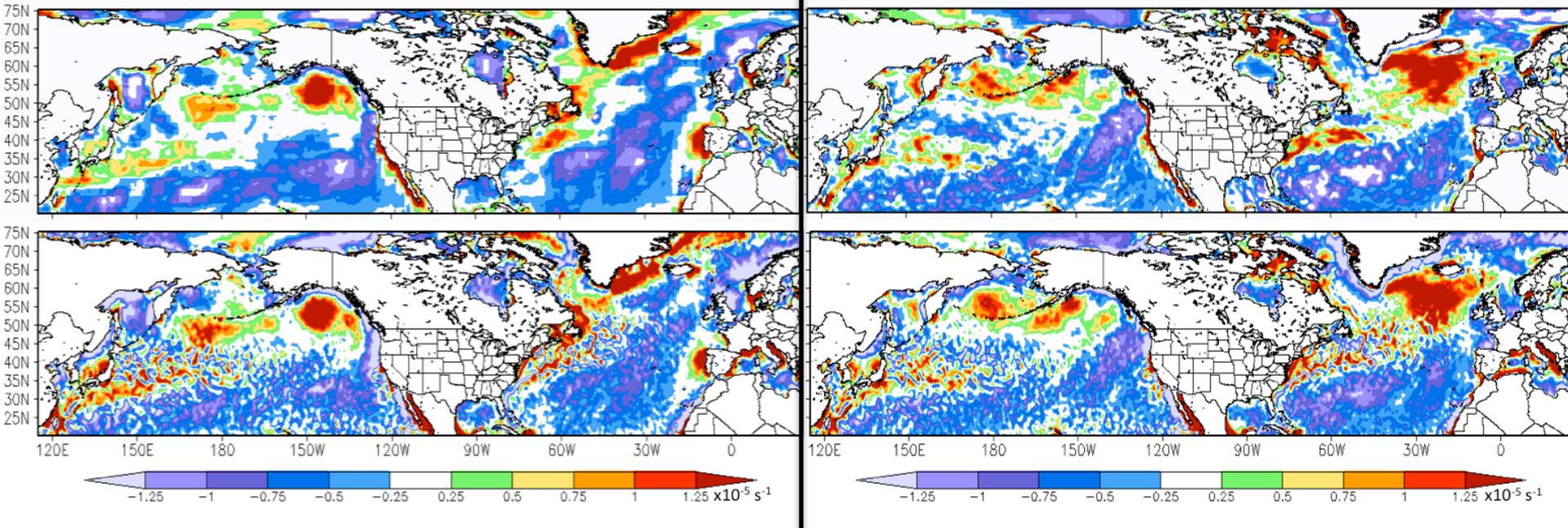


- Example gradients of Reynolds SSTs (K/100km).
  - These fields are noisy and require smoothing
  - Smoothing can be tuned to match the spatial scales in wind observations.

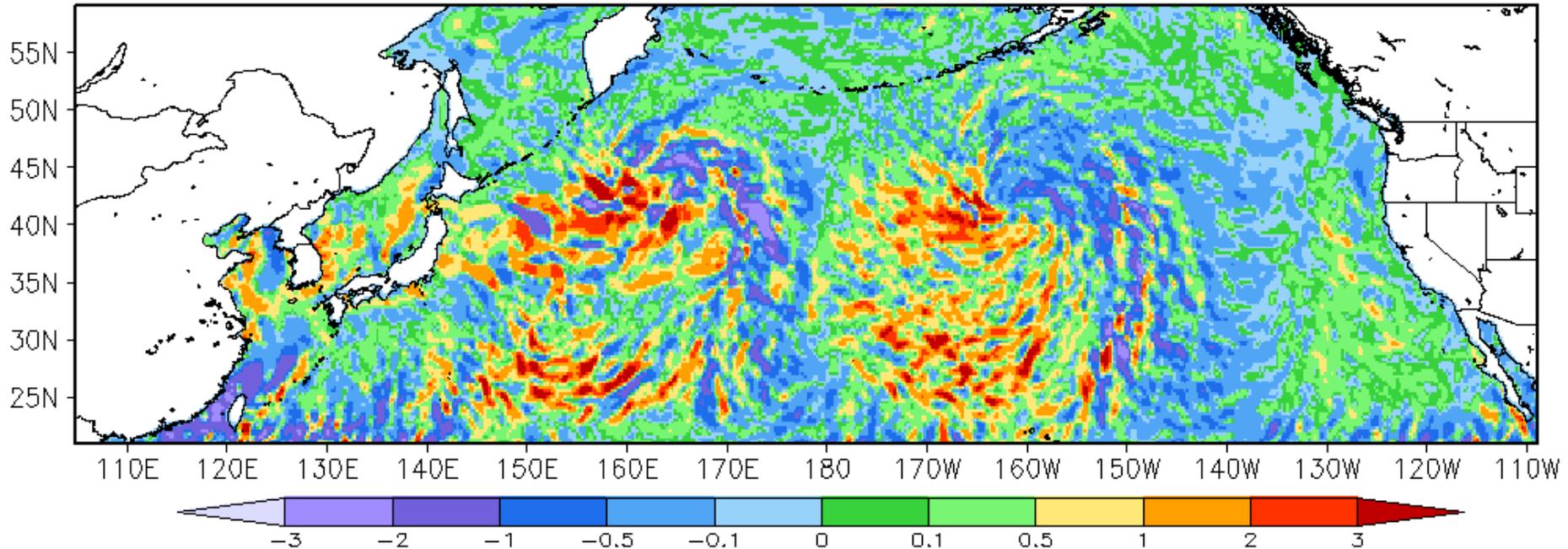
# CCMP (top) vs. FSU (bottom): Curl

June **1988**: 1 Satellite Source

June **2003**: 7 Satellite Sources

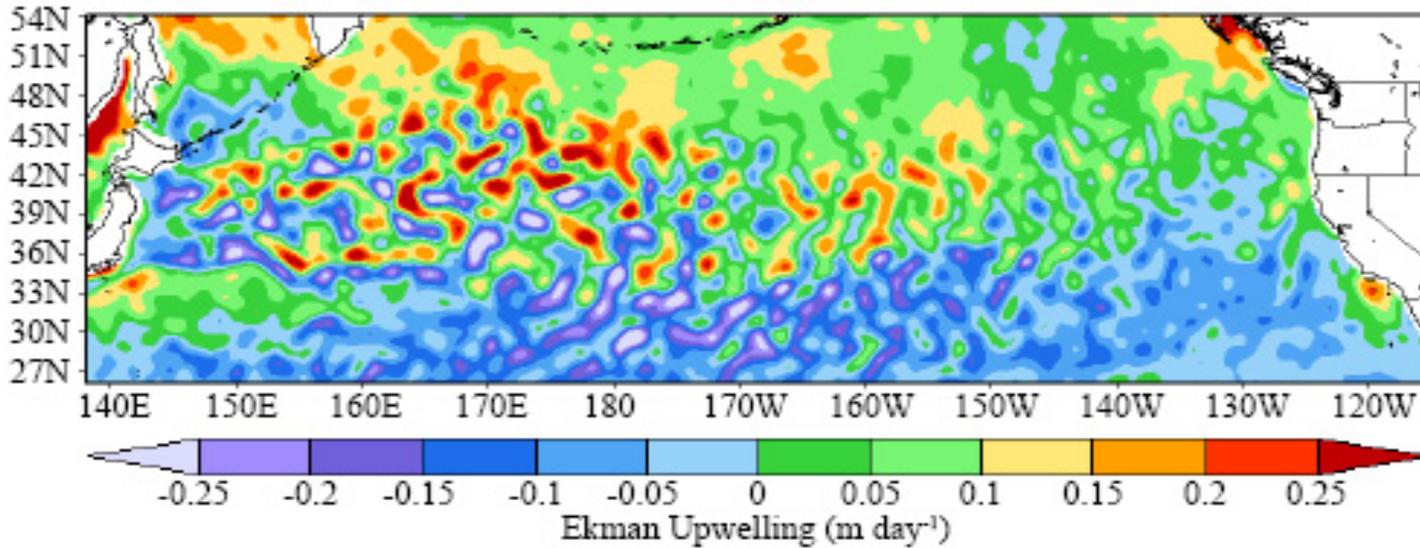


# Example Change in Surface Wind Speed

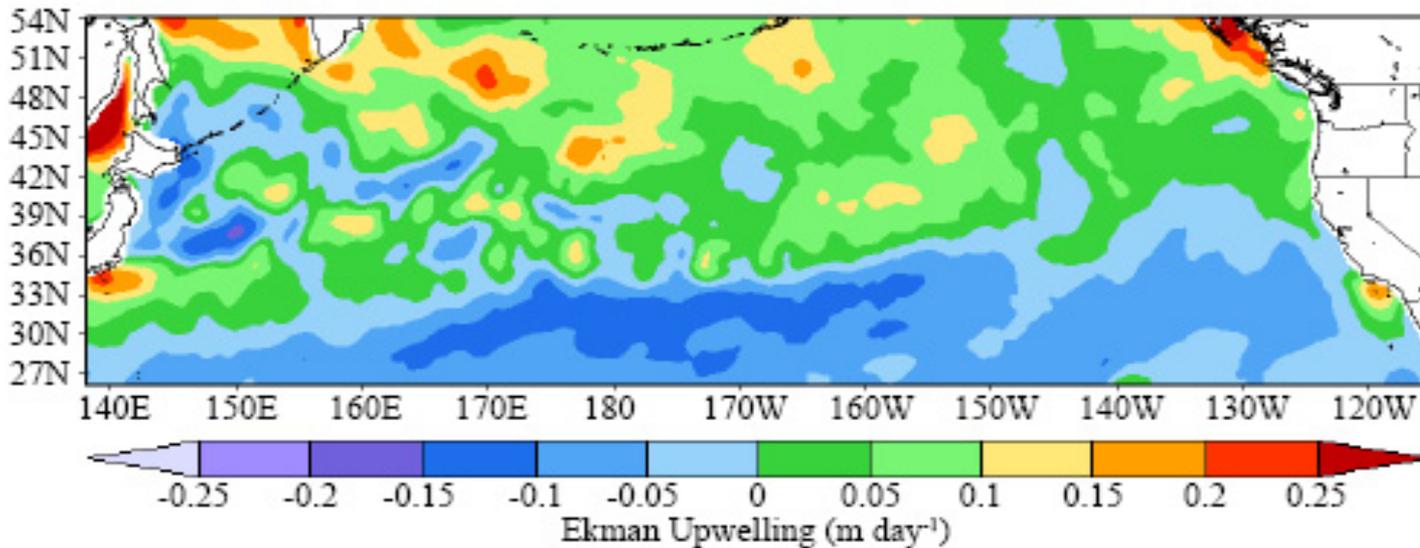


- Change in surface wind speed ( $\text{ms}^{-1}$ ) due to above SST gradients (Reynolds SSTs).
  - These changes are largely observed in OVW swaths
  - SST gradient must be considered to add such features in areas with only speed data and in data voids

# Ekman Upwelling



Baroclinic



Control